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# Reducing Energy Consumption in Wireless Sensor Networks

CHES seminar  
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## Introductory Overview

Minimum Energy Coding

Radio Power Control

Bit Error Rate

Energy Consumption

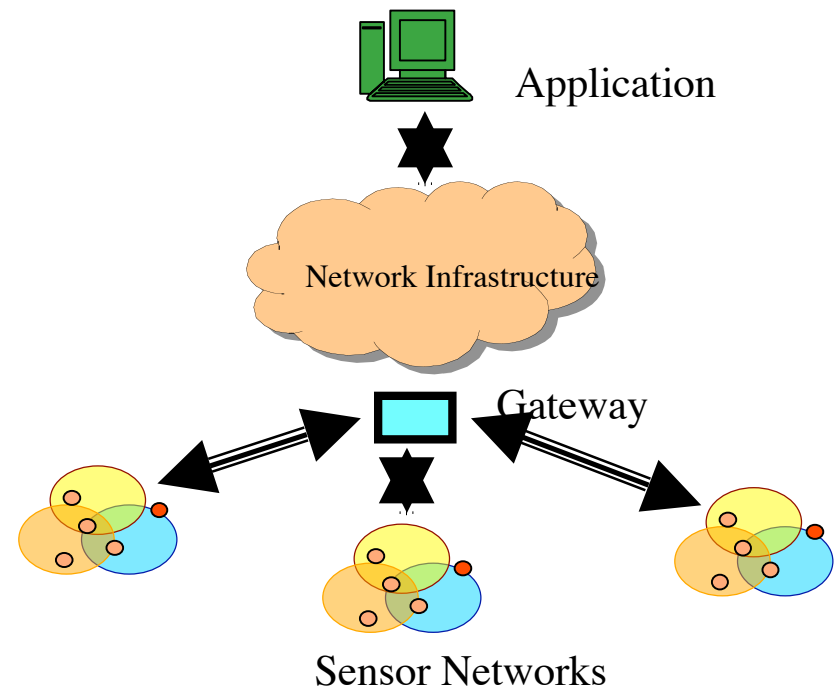
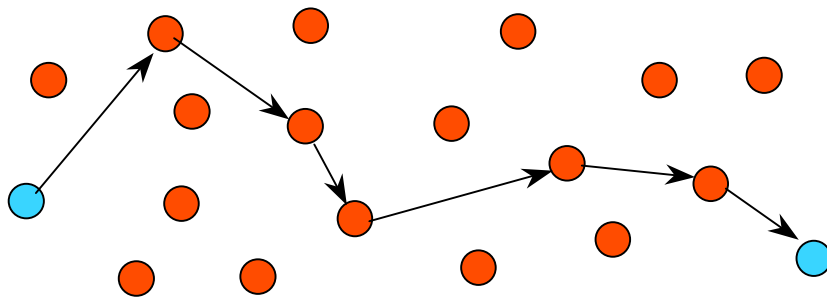
Numerical Results

Conclusions and Future Work



# Definition of WSNs

“Wireless Sensor Networks (WSNs) are networks for communication, control, sensing and actuation by small nodes communicating through wireless links”

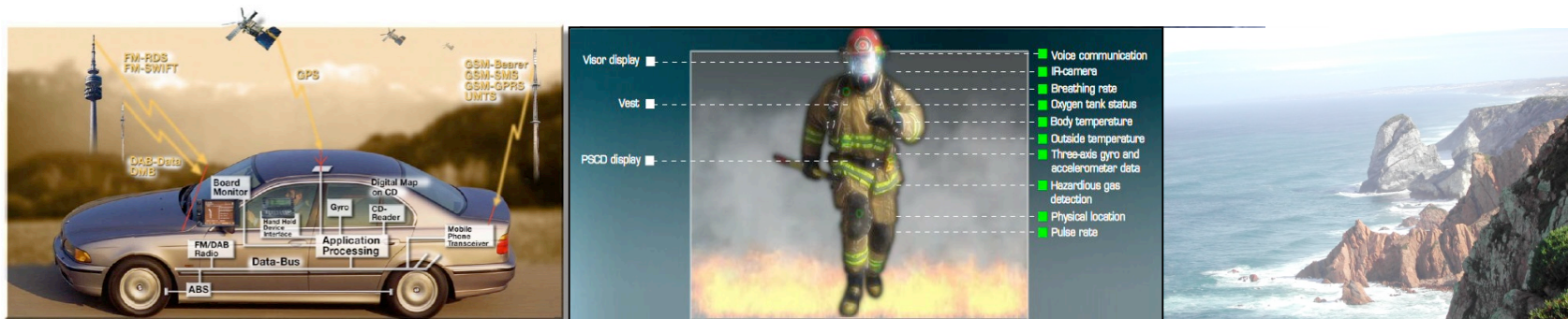
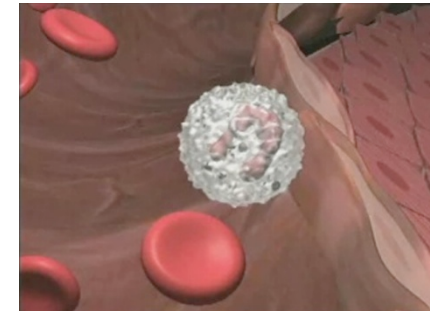




# Applications

Tremendous space of applications:

- Monitoring space: ocean water, pollution, ...
- Monitoring things: robots, human body, ...





# History of WSNs



DARPA DSN node (~1960)

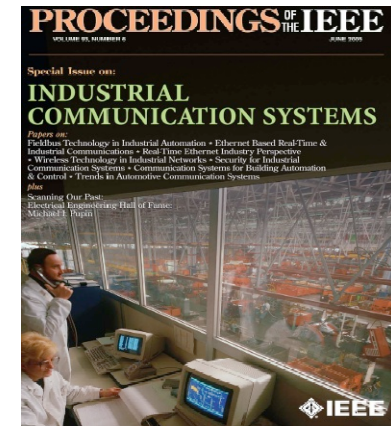


Mica node (~2000)



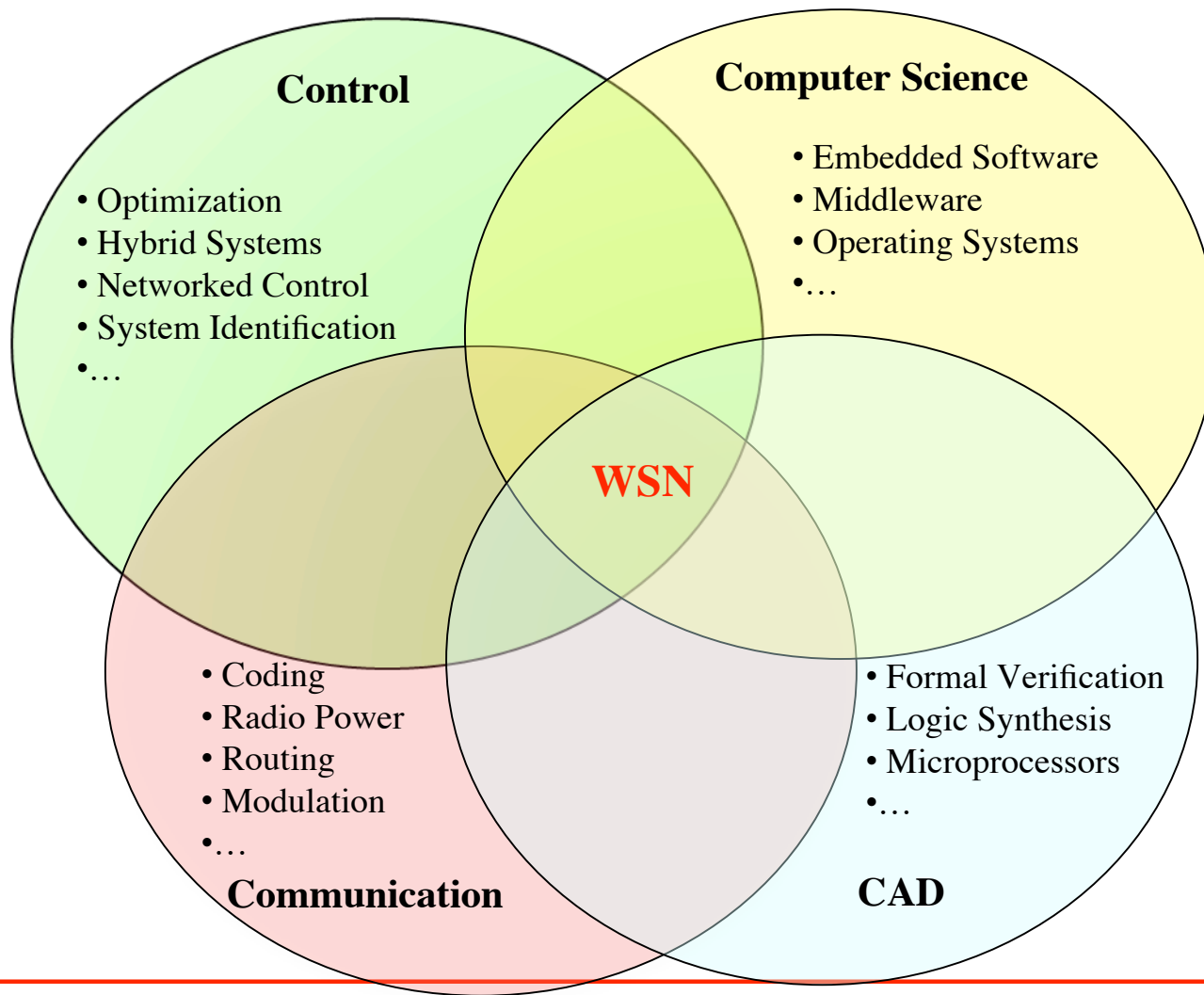
Tmote-sky node (~2003)

- WSNs are an area of active research from electronic to computer science since few years.
- Many industries are now investing in this new technology:
  - ABB
  - Fiat
  - Pirelli
  - Siemens
  - United Technology
  - ...





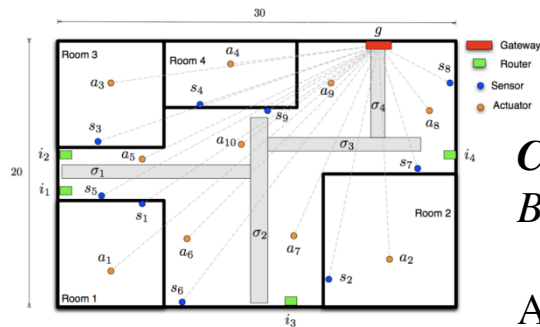
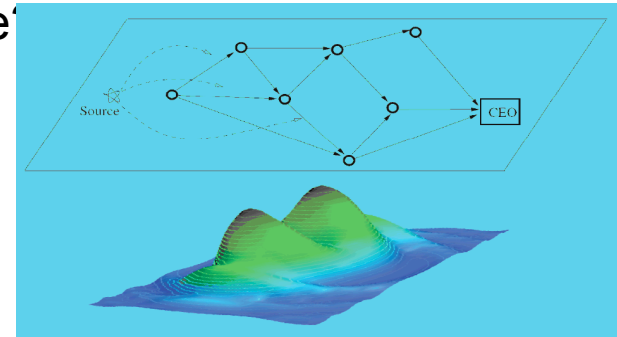
# Design Principles of WSNs





# Some Challenges...

- ♣ How to schedule the link each node should select to forward packets?
- ♣ How to quantize the measurements to transmit the minimum amount of information in the presence of uncertainties of the network?
- ♣ How to do radio power and rate control, when neither accurate channel models and channel state information are available?
- ♣ How to access to the channel?



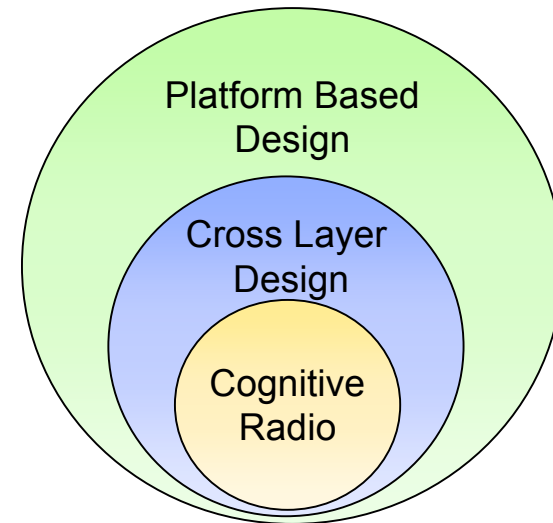
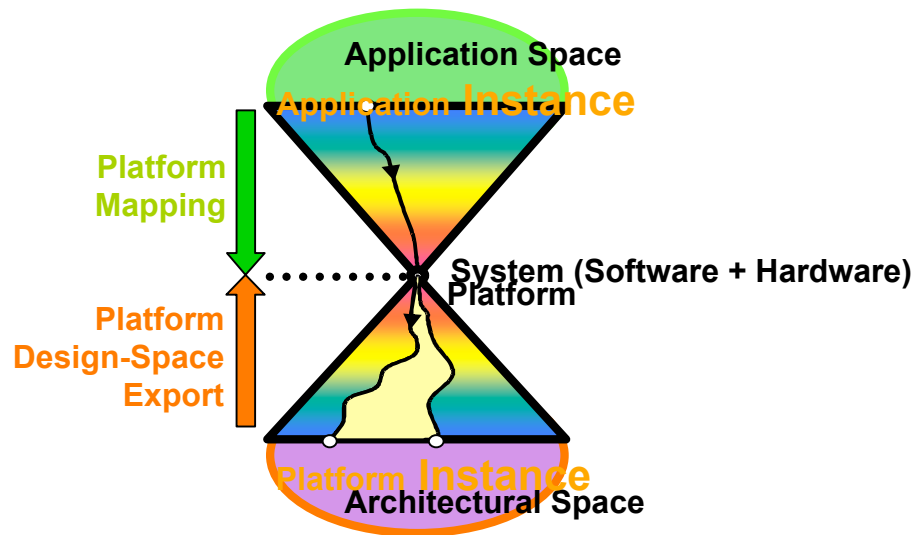
*COSI project: Synthesis of Embedded Networks for Building Automation and Control*

A. Pinto & A. Sangivanni-Vincentelli, UC Berkeley



# Design Principles of WSNs...

- ♣ Design of WSNs includes several techniques (distributed computation, distributed source coding, distributed control,...).
- ♣ Cross-layer approaches are necessary to take into account several interacting techniques and protocols.



A. Sangiovanni-Vincentelli et al.





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Introductory Overview  
**Minimum Energy Coding**  
Radio Power Control  
Bit Error Rate  
Energy Consumption  
Numerical Results  
Conclusions and Future Work



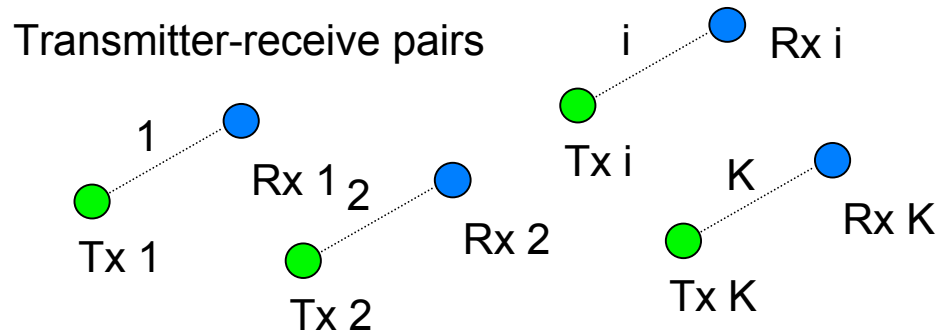
# Minimum Energy Coding

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- ♣ Performance analysis of minimum energy coding schemes in Coded Division Multiple Access (CDMA) wireless sensor networks:
  1. **Minimum Energy coding (ME);**
  2. **Modified Minimum Energy coding (MME).**
  
- ♣ Detailed models of the **energy consumption** and **bit error rate**:
  1. coding schemes;
  2. wireless channel;
  3. power control;
  4. hardware characteristics of the transceivers.

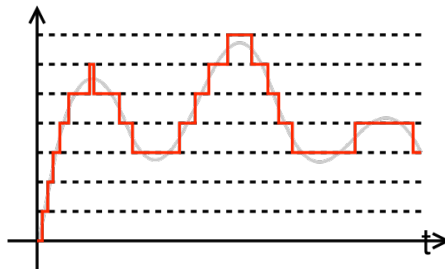
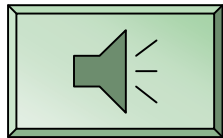


# System Description



- ♣ Data sensed by a node are coded with a Minimum Energy coding scheme.
- ♣ The bits of the ME coded data are OOK modulated: only bits having value 1 are transmitted after a DS-CDMA spreading operation.

Source

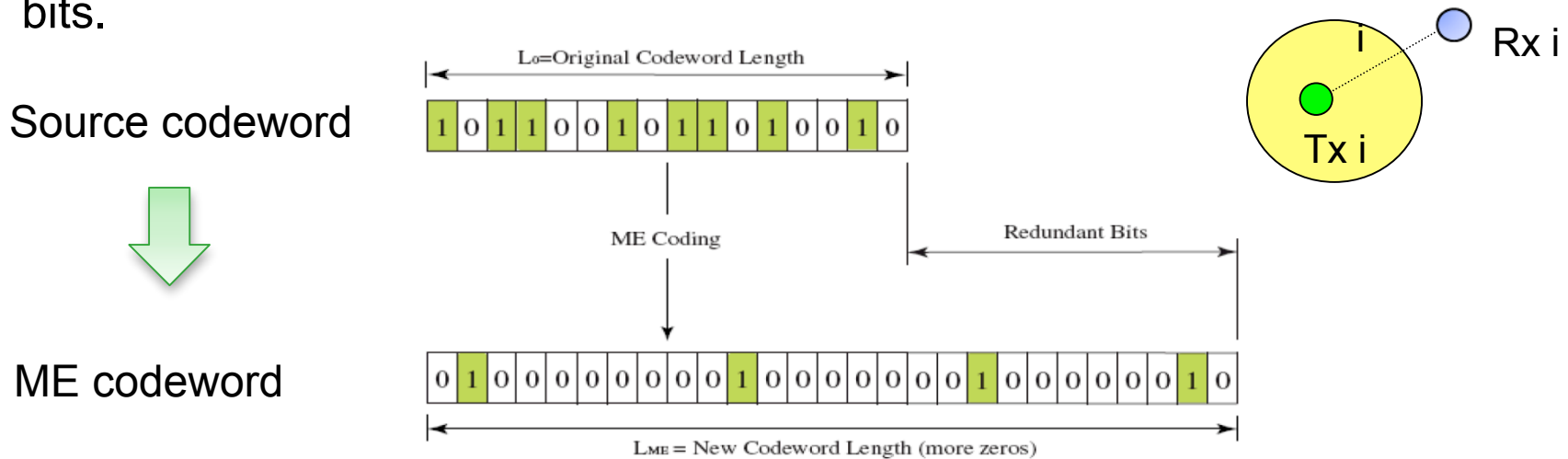


100111  $\longrightarrow$  1000010000  
Source Codeword                      ME Codeword



# ME Coding

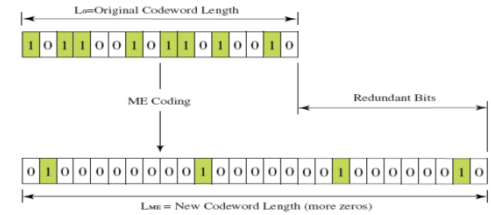
- ♣ In ME Coding (Erin and Asada: “Energy Optimal Codes for Wireless Communications” in 38th IEEE CDC 99) a source codeword is mapped into a new codeword having larger length but less number of 1 (or high) bits.



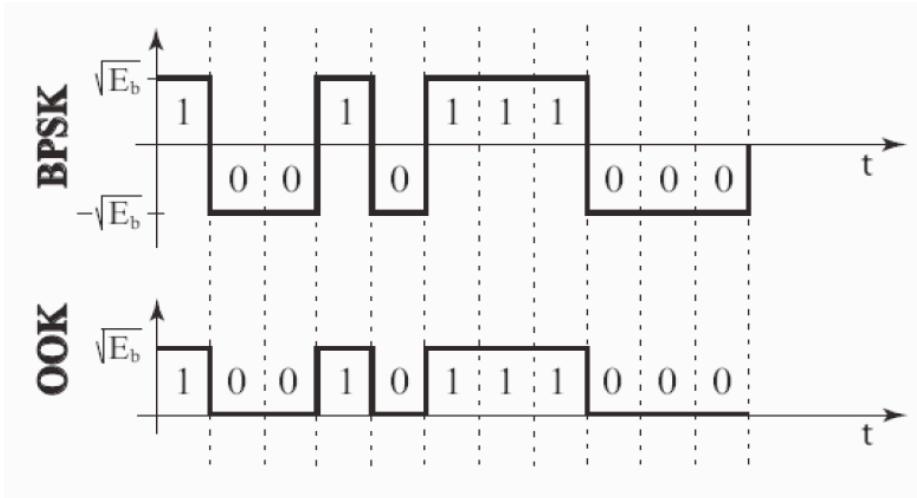
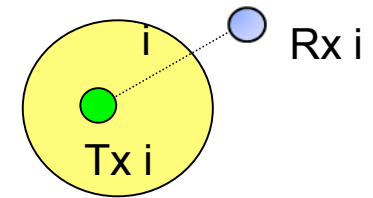
- ♣ Source codewords having large probability of occurrence are associated to ME codewords with less high bits.
- ♣ Only high bits are transmitted with OOK modulation.



# OOK Modulation



♣ Only bits having value 1 are transmitted



←  $\alpha = 1$

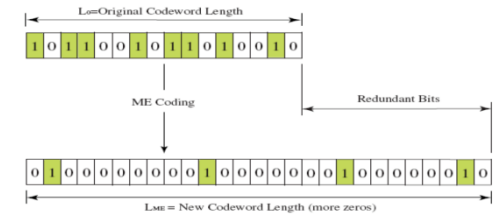
←  $\alpha < 1$

- Lower Activity
- Lower interference
- Higher bit error rate

♣  $\alpha$  is the average transmit time per codeword.



## ME Coding (2)



### ♣ Energy consumption per ME codeword

$$\begin{aligned} E_i^{(ME)} &= E_i^{(tx)} + E_i^{(rx)} \\ &= P^{(tx,ckt)} \left( T^{(on,tx,ME)} + T_s \right) + \alpha_{ME} P_i T^{(on,tx,ME)} + P^{(rx,ckt)} \left( T^{(on,rx,ME)} + T_s \right) \end{aligned}$$

### ♣ ME coding increases the value of three system parameters:

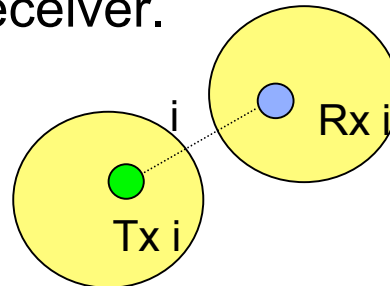
1. the codeword length;
2. the Transmitter active time (it is negligible with respect to the radio power consumption);
3. the Receiver active time: it is not negligible, the power spent to receive is approximately the same as that used to transmit.



# MME Coding

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- ♣ MME coding exploits a structure of the codeword that allows the **receiver to go in a sleep state**: Kim and Andrews: “*An Energy Efficient Source Coding and Modulation Scheme for Wireless Sensor Networks*”. In IEEE WSPAWC, 2005.
- ♣ In MME coding, energy is saved not only at the transmitter as ME coding, but also at the receiver.

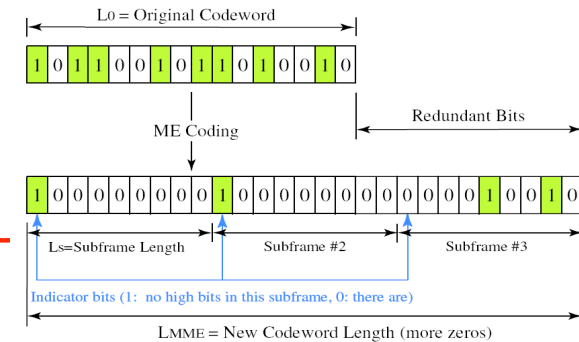








# MME Coding (3)



- ♣ MEE energy consumption per codeword:

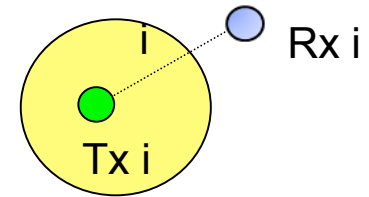
$$\begin{aligned}
 E_i^{(MME)} &= E_i^{(tx)} + E_i^{(rx)} \\
 &= P^{(tx,ckt)} \left[ T^{(on,tx,MME)} + T_s \right] + \alpha_{MME} P_i T^{(on,tx,MME)} + \\
 &\quad + P^{(rx,ckt)} \left[ T^{(on,rx,MME)} + (N_i + 1) T_s \right] .
 \end{aligned}$$

- ♣  $N_i$  average receiver activity (it is a function of the number of sub-frames, and bit error rate)

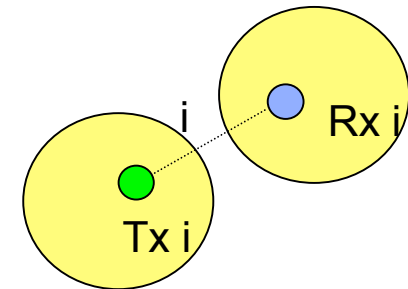


# Energy of ME and MME

$$\begin{aligned} E_i^{(ME)} &= E_i^{(tx)} + E_i^{(rx)} \\ &= P^{(tx,ckt)} \left( T^{(on,tx,ME)} + T_s \right) + \alpha_{ME} P_i T^{(on,tx,ME)} + P^{(rx,ckt)} \left( T^{(on,rx,ME)} + T_s \right) \end{aligned}$$



$$\begin{aligned} E_i^{(MME)} &= E_i^{(tx)} + E_i^{(rx)} \\ &= P^{(tx,ckt)} \left[ T^{(on,tx,MME)} + T_s \right] + \alpha_{MME} P_i T^{(on,tx,MME)} + \\ &\quad + P^{(rx,ckt)} \left[ T^{(on,rx,MME)} + (N_i + 1) T_s \right] . \end{aligned}$$





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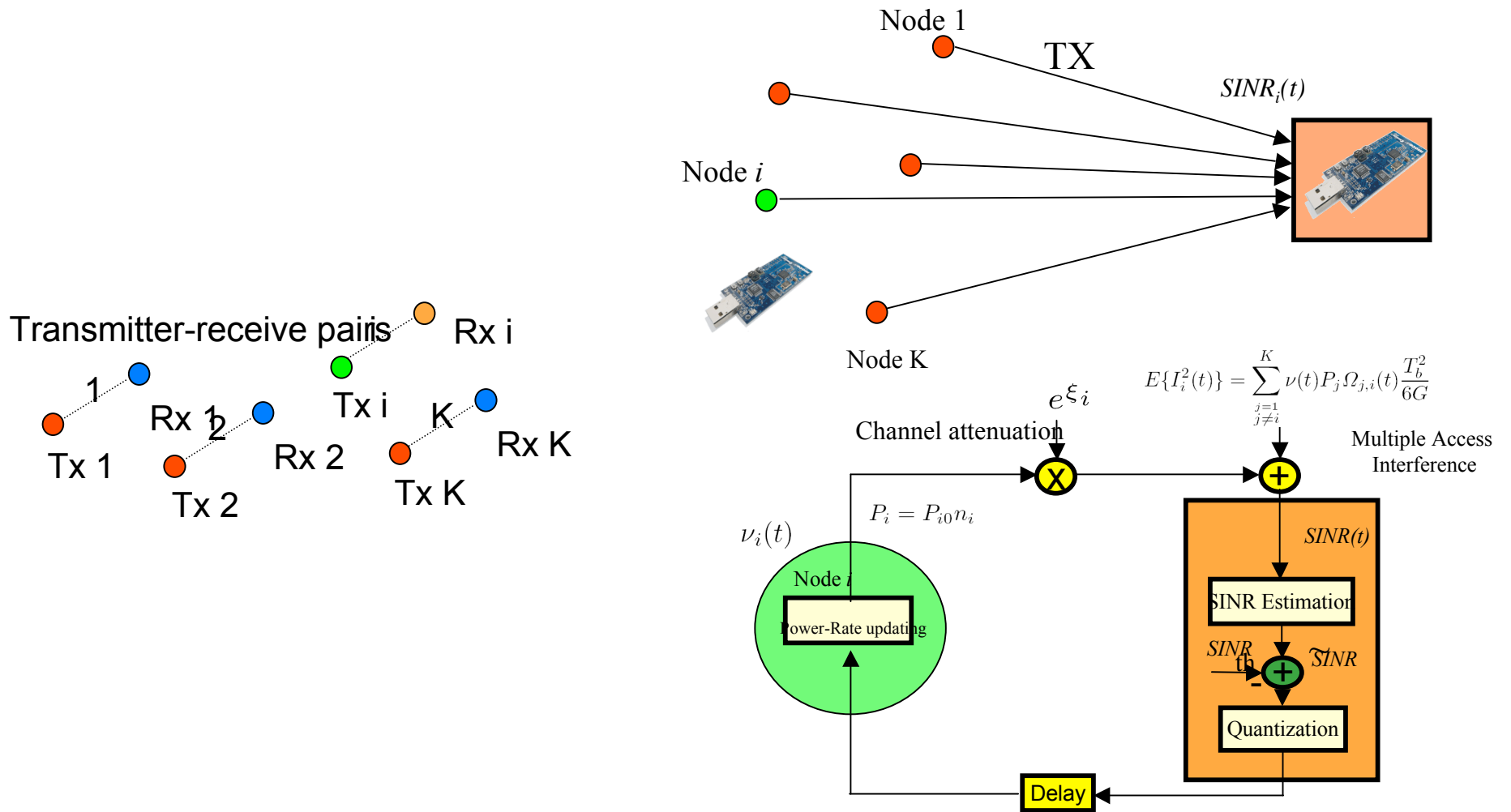
# Radio Power Control

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- ♣ Efficient power control algorithms for wireless sensor networks (WSNs) are crucial to **reduce energy consumption**.
  - **Lifetime**: in scenario where recharging is not possible, radio power control is very important to increase the network lifetime.
  - **Collisions**: power control is beneficial to reduce packet collisions (more retransmitted packets means wasting energy), and increase throughput.
- ♣ Energy for radio power is responsible from **37%** up to **85%** of the **total Energy** consumption for off-the-shelf sensor nodes.

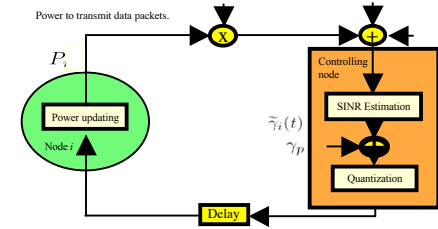


# Radio Power Control (2)



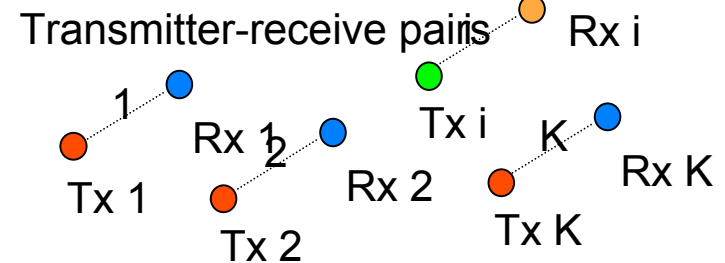


# Radio Power Control (3)



♣ Received signal

$$Z_i(t) = D_i(t) + I_i(t) + N_g(t)$$



$$D_i(t) = \sqrt{\frac{h_{i,i}(t)P_i}{2}} T_b b_i(t)$$

Desired Signal

$$E\{I_i^2(t)\} = \sum_{\substack{j=1 \\ j \neq i}}^K \nu(t) P_j \Omega_{j,i}(t) \frac{T_b^2}{6G}$$

MAI

$$N_g(t)$$

Thermal Noise

$$\Pr(\nu(t) = 1) = \alpha$$

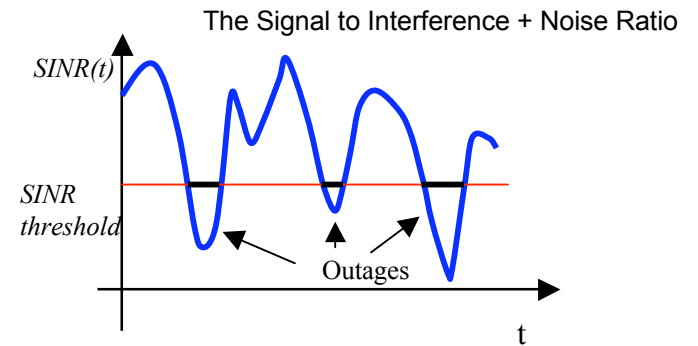
Transmitter Activity (ME or MME)



# The SINR

- ♣ The SINR of the signal of a node is expressed as

$$\text{SINR}_i(t) = \frac{b_i(t)h_{i,i}(t)P_i}{\frac{N_0}{2T_b} + \frac{1}{3G} \sum_{\substack{j=1 \\ j \neq i}}^K \nu_j(t)h_{ji}(t)P_j}$$

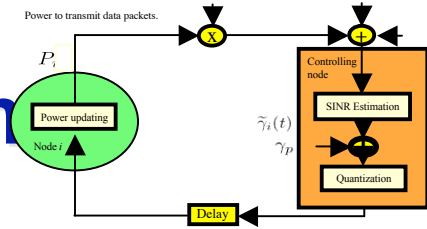


$$\boldsymbol{\nu}(t) = [\nu_1(t), \dots, \nu_K(t)]^T$$

Vector of Binary on/off Processes:  
ME and MME coding

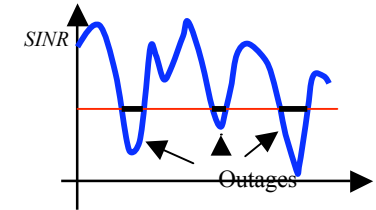


# The Optimization Problem



## ♣ Mixed integer-real optimization problem

$$\begin{aligned}
 \max_{\mathbf{n}, \mathbf{P}} \quad & \sum_{i=1}^K n_i \\
 \text{s.t.} \quad & \Pr [SINR_i(\boldsymbol{\xi}, \boldsymbol{\nu}) < \gamma_i] \leq \bar{P}_{out}^i \\
 & \sum_{i=1}^K P_i \leq P_T \\
 & 0 < P_{i0} \\
 & 1 \leq n_i \leq G_{i0}, \quad n_i \in \mathbb{N}, i = 1, \dots, K
 \end{aligned}$$



$$\mathbf{P} = [P_{01}, \dots, P_{0K}]^T \quad P_i = P_{i0} n_i, \quad i = 0, \dots, K$$

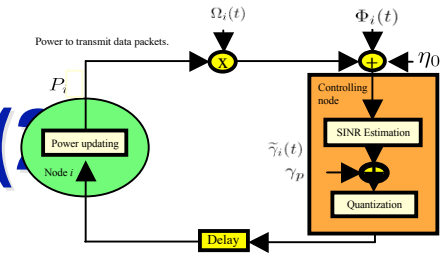
$$\mathbf{n} = [n_1, n_2, \dots, n_K]^T$$

- K.-L. Hsiung, S.-J. Kim, S. Boyd, "Power Control in Lognormal Fading Wireless Channel with Uptime Probability Specifications via Robust Geometric Programming", ACC 2005.
- J. Papandriopoulos, J. Evans, S. Dey, "Outage-Based Power Control for Generalized Multiuser Fading Channels", IEEE Trans. Comm. 2006.





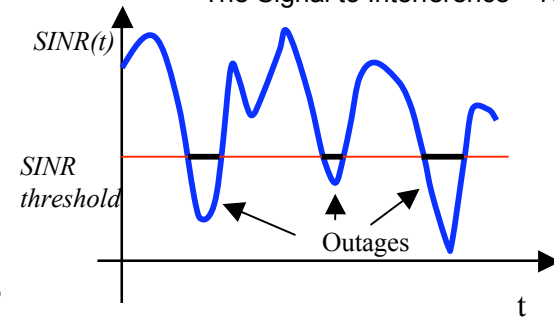
# The Optimization Problem (I)



♣ How to express the constraints on the outage probability?

$$Pr [SINR_i(\xi, \nu) < \gamma_i] = \int_0^{\gamma_i} f_{SINR_i}(x) dx$$

The Signal to Interference + Noise Ratio

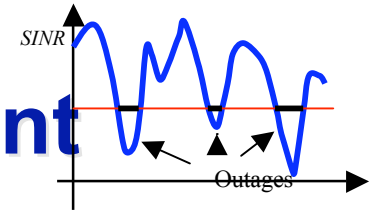


♣ How to solve efficiently the problem?

- good precision of the solution (otherwise waste of resources);
- computationally affordable (WSNs have limited processing capabilities).



# Outage Probability Constraint



- The SINR is a combination of log-normal processes weighted with on/off binary random processes, it is approximated with an overall Log-normal:

$$SINR_i(\xi(t), \nu(t)) = L_i(\xi(t), \nu(t))^{-\frac{1}{2}} \implies L_i(\xi(t), \nu(t)) \cong e^{Z_i(t)} \implies Z_i \in G(m_{Z_i}, \sigma_{Z_i})$$

$$m_{Z_i} = \ln \left[ \frac{M_{m1}^2}{\sqrt{M_{m2}}} \right] \quad M_{m1} \triangleq E_{\xi(t), \nu(t)} \{ SINR(\xi(t), \nu(t)) \} ,$$

$$\sigma_{Z_i}^2 = \ln \left[ \frac{M_{m2}}{M_{m1}^2} \right] \quad M_{m2} \triangleq E_{\xi(t), \nu(t)} \{ SINR^2(\xi(t), \nu(t)) \}$$

Fischione, Graziosi, Santucci,  
IEEE Trans. Comm., October 2007

$$Pr[SINR_i(\xi, \nu) < \gamma_i] = Q \left( \frac{-2 \ln \gamma_i - m_{Z_i}}{\sigma_{Z_i}} \right) \quad Q(x) = 1/\sqrt{2\pi} \int_x^\infty e^{-t^2/2} dt$$



$$\frac{P_{i0}}{I_i(\mathbf{n}, \mathbf{P}_{-i})} \geq \gamma_i^2$$

Interference Function

$$I_i(\mathbf{n}, \mathbf{P}_{-i}) = \frac{G_i(\mathbf{P}_{-i})^{q_i - \frac{1}{2}}}{H_i(\mathbf{P}_{-i})^{2q_i - 2}}$$

$$q_i = Q^{-1}(\bar{P}_{out}^i)$$

$$H_i(\mathbf{n}, \mathbf{P}_{-i}) = M_{m1} P_{i0}$$

$$G_i(\mathbf{n}, \mathbf{P}_{-i}) = M_{m2} P_{i0}^2$$



# Relaxation Problem

## ♣ Main Problem

$$\begin{aligned}
 & \max_{\mathbf{n}, \mathbf{P}} \sum_{i=1}^K n_i \\
 \text{s.t. } & \frac{P_{i0}}{I_i(\mathbf{n}, \mathbf{P}_{-i})} \geq \gamma_i^2 \quad \forall i = 1, \dots, K \\
 & \sum_{i=1}^K n_i P_{i0} \leq P_T \\
 & P_{i0} > 0 \quad \forall i = 1, \dots, K \\
 & 1 \leq n_i \leq G_i, \quad n_i \in \mathbb{N}^+ \quad \forall i = 1, \dots, K
 \end{aligned}$$



## The Relaxation Problem

$$\begin{aligned}
 & \min_{\mathbf{P}} \sum_{i=1}^K n_i P_{i0} \\
 \text{s.t. } & \frac{P_{i0}}{I_i(\mathbf{n}, \mathbf{P}_{-i})} \geq \gamma_i^2 \quad \forall i = 1, \dots, K \\
 & P_{i0} > 0 \quad \forall i = 1, \dots, K \\
 & 1 \leq n_i \leq G_i, \quad n_i \in \mathbb{N}^+ \quad \forall i = 1, \dots, K
 \end{aligned}$$

♣ Any pair of vector  $\bar{\mathbf{P}}$  and  $\bar{\mathbf{n}}$  that solves the relaxation problem, with a cost function  $P_T$  then provides a feasible solution of the original problem.

♣ **Proposition 1:**  $\bar{n}_i \leq \tilde{n}_i \implies I_i(\bar{\mathbf{n}}, \mathbf{P}) \leq I_i(\tilde{\mathbf{n}}, \mathbf{P})$  for  $\mathbf{P}$  and  $i$ .

♣ **Theorem:** If the pair  $(\bar{\mathbf{n}}, \bar{\mathbf{P}})$  is a solution of the relaxation problem, then it verifies the following equations.

$$\frac{P_{i0}}{I_i(\bar{\mathbf{n}}, \bar{\mathbf{P}}_{-i})} = \gamma_i^2 \quad \forall i = 1, \dots, K$$



# Branch-and-bound Solution

- ♣ **Proposition 2:**  $\bar{\mathbf{n}}$  is feasible  $(\mathbf{n}, \mathbf{P})$  pair can be a solution of the original problem only if  $\|\mathbf{n}\|_1 \geq \|\bar{\mathbf{n}}\|_1$

The proposition says that, given a feasible vector  $\bar{\mathbf{n}}$ , the search for the feasible solution can be restricted to the set  $\mathcal{N}_\Sigma(\bar{\mathbf{n}}) = \mathcal{N} \setminus \{ \mathbf{n} \text{ such that } \|\mathbf{n}\|_1 \leq \|\bar{\mathbf{n}}\|_1 \}$

- ♣ **Proposition 3:** if  $\bar{\mathbf{n}}$  is infeasible, then any  $\mathbf{n}$  such that  $\|\mathbf{n}\|_1 \leq \|\bar{\mathbf{n}}\|_1$  is infeasible as well.

The proposition says that, if  $\bar{\mathbf{n}}$  is infeasible, the set of infeasible solutions can be restricted to  $\mathcal{N}_\mathcal{I}(\bar{\mathbf{n}}) = \mathcal{N} \setminus \{ \mathbf{n} \text{ such that } \|\mathbf{n}\|_1 \geq \|\bar{\mathbf{n}}\|_1 \}$



# Radio Power Control (4)

- ♣ T Relaxation Problem is solved by contraction mappings (Fischione, Butussi, IEEE ICC 2007)

$$\begin{aligned} \min_{\mathbf{P}} \quad & \sum_{i=1}^K n_i P_{i0} \\ \text{s.t.} \quad & \frac{P_{i0}}{I_i(\mathbf{n}, \mathbf{P}_{-i})} = \gamma_i^2 \quad \forall i = 1, \dots, K \\ & P_{i0} > 0 \quad \forall i = 1, \dots, K \\ & 1 \leq n_i \leq G_i, \quad n_i \in \mathbb{N}^+ \quad \forall i = 1, \dots, K \end{aligned}$$

Algorithm *Relaxation Problem*

```
1:  $t := 0$ ;  
2:  $\mathbf{n}(t-1) := \mathbf{1}$  ;  
3:  $\mathbf{p}(t-1) := \mathbf{0}$ ;  
4:  $\mathbf{n}(t) := \mathbf{1}$  ;  
5:  $\mathbf{p}(t) := \mathbf{p}_0$  ;  
6: while  $\|\mathbf{p}(t) - \mathbf{p}(t-1)\|_2 \geq \varepsilon$  do  
7:   for  $i := 1 : K$  do  
8:      $p_i(t) := I_i(\mathbf{n}_{-i}(t-1), \mathbf{p}_{-i}(t-1))\gamma_i$   
9:   end for;  
10:   $t := t + 1$ ;  
11: end while;
```

- ♣ A branch-and-bound algorithm builds the set of feasible and unfeasible rates by solving the Relaxation Problem, collecting feasible solutions, and reducing the candidate solutions via Proposition 2 and 3.
- ♣ It can be proved that the algorithm converges within a random time shorter than an exhaustive search over the initial set of possible rates.

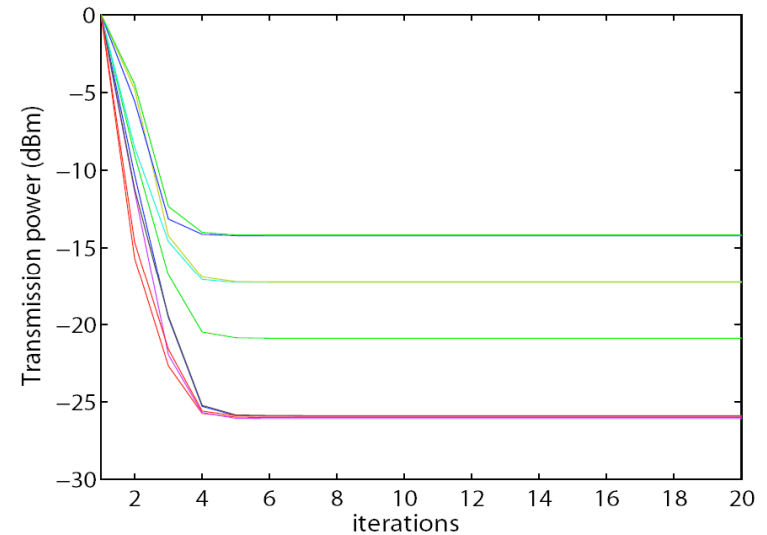


# Numerical Results for Power Control

Scenario	$\sigma_{\xi_i}$	$\alpha_i$
A	0.5, 0.5, 0.5, 0.5	0.4, 0.4, 0.4, 0.4
B	0.5, 0.5, 0.5, 0.5	0.2, 0.2, 0.2, 0.2
C	0.5, 0.5, 0.5, 0.5	0.7, 0.7, 0.7, 0.7
D	0.4, 0.4, 0.4, 0.4	0.4, 0.4, 0.4, 0.4
E	0.6, 0.6, 0.6, 0.6	0.4, 0.4, 0.4, 0.4
M	0.5, 0.6, 0.4, 0.6	0.2, 0.4, 0.2, 0.7

Number of rate vectors explored (solutions of the Relaxation Problem) to get the optimal solution with our proposed method:

Scenario	min	max	average
A	46	247	150
B	84	247	153
C	47	238	137
D	84	247	149
E	47	247	141
M	31	222	103



Convergence of the Relaxation Problem

An exhaustive search over all rate vectors would have required  $9^4 = 6561$  solutions of the relaxation problem.



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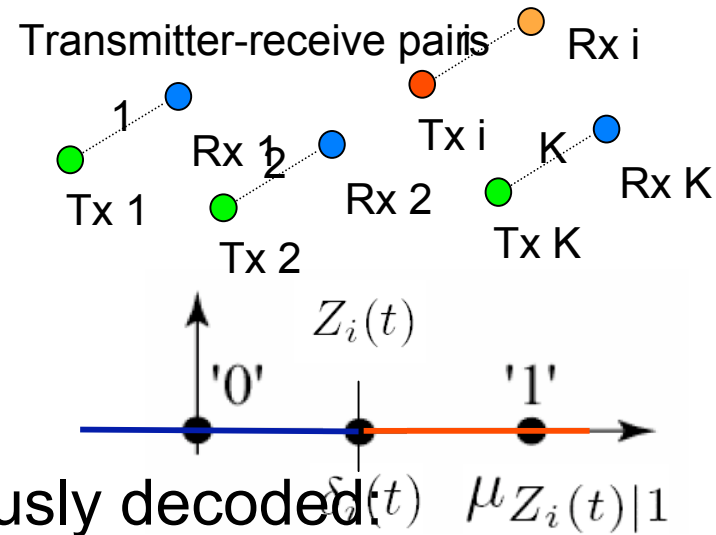
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# Bit Error Rate

- ♣ Decision variable at the receiver

$$Z_i(t) = D_i(t) + I_i(t) + N_g(t)$$



- ♣ The decision variable is erroneously decoded:
  - as a high bit, when a low bit was transmitted:

$$p_{i|0} = \Pr [Z_i(t) \geq \delta_i | b_i(t) = 0, \mathbf{h}_i(t), \nu_j(t)]$$

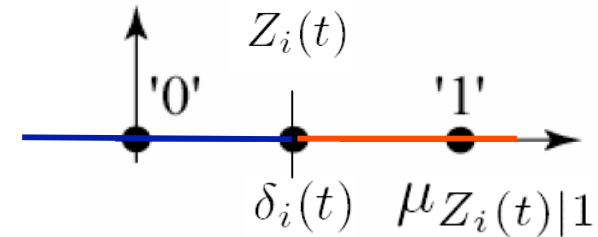
- as a low bit when a high bit was transmitted:

$$p_{i|1} = \Pr [Z_i(t) < \delta_i | b_i(t) = 1, \mathbf{h}_i(t), \nu_j(t)]$$





# Bit Error Rate (2)



- The probabilities are computed adopting the usual standard Gaussian approximation, where  $Z_i(t)$  is modelled as a Gaussian random variable conditioned to the distribution of the channel coefficients and coding.

$$Z_i(t) \sim \mathcal{N}(\mu_{Z_i(t)}, \sigma_{Z_i(t)})$$



$$p_{i|0} = Q\left(\frac{\delta_i(t)}{\sigma_{Z_i(t)}}\right),$$

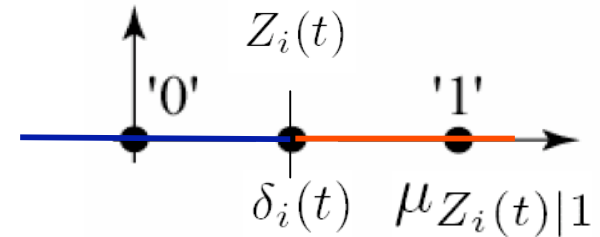
$$p_{i|1} = Q\left(\frac{\mu_{Z_i(t)|1} - \delta_i(t)}{\sigma_{Z_i(t)}}\right)$$

$$\mu_{Z_i(t)} = \begin{cases} \mu_{Z_i(t)|0} = 0 & \text{if } b_i(t) = 0 \\ \mu_{Z_i(t)|1} = \sqrt{\frac{P_i \Omega_{i,i}(t)}{2}} T_b^2 & \text{if } b_i(t) = 1 \end{cases}$$

$$\sigma_{Z_i(t)} = \sqrt{\frac{N_0 T_b}{4} + \sum_{\substack{j=1 \\ j \neq i}}^K \nu(t) P_j \Omega_{j,i}(t) \frac{T_b^2}{6G}}$$



## Bit Error Rate (4)



- ♣ The Bit error probability is computed using the Log Normal SINR expression, and the Stirling approximation for the statistical Expectation:

$$\Phi_i(\delta_i) \approx \frac{2}{3} [(1 - \alpha_i)Q(\mu_{\zeta_{i0}}) + \alpha_i Q(\mu_{\zeta_{i1}})] + \frac{1}{6} \left[ (1 - \alpha_i)Q\left(\mu_{\zeta_{i0}} + \sqrt{3}\sigma_{\zeta_{i0}}\right) + (1 - \alpha_i)Q\left(\mu_{\zeta_{i0}} - \sqrt{3}\sigma_{\zeta_{i0}}\right) + \alpha_i \right].$$

- ♣ It can be proved that the BER is a convex function.
  - The gradient method is used to derive the **optimal decision threshold**.



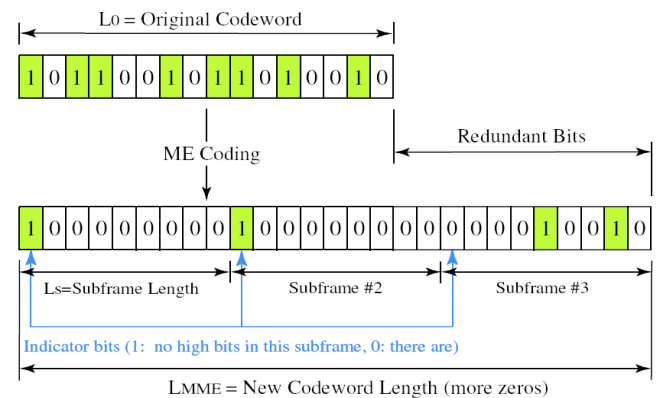
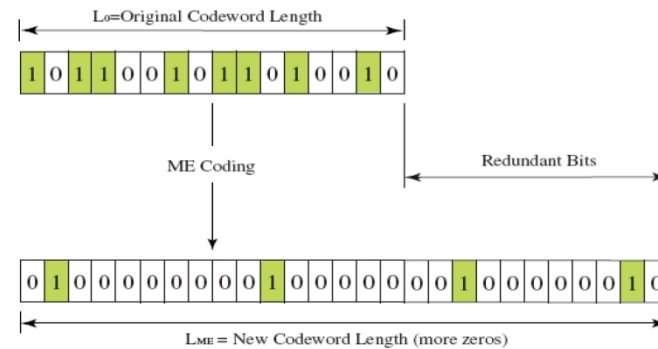
# Bit Error Rate of ME and MME

The characterization  $\Phi_i$  of can be used to compute the BER of

1. ME:  $\alpha = \alpha_{ME}$

2. MME: the coding structure,

$$\alpha = \alpha_{MME}$$



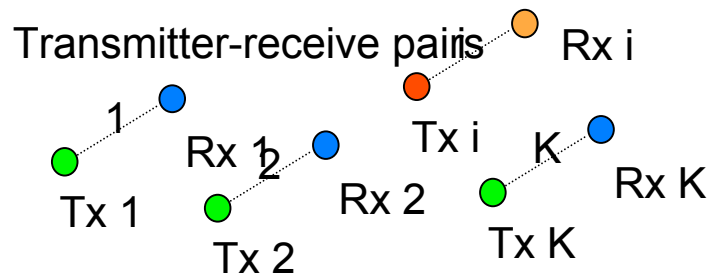


- 
- ♣ Introductory Overview
  - ♣ Main Contribution
  - ♣ System Description
  - ♣ Radio Power Control
  - ♣ Bit Error Rate
  - ♣ **Energy Consumption**
  - ♣ Numerical Results
  - ♣ Conclusions and Future Work

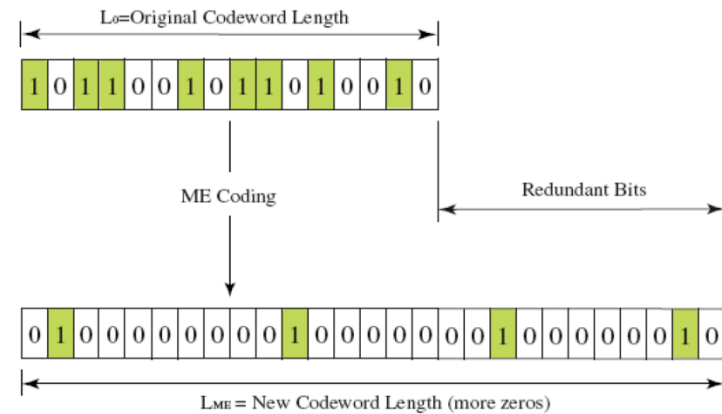


# Average ME Energy Consumption

$$\begin{aligned}
 E_i^{(ME)} &= E_i^{(tx)} + E_i^{(rx)} \\
 &= P^{(tx,ckt)} \left( T^{(on,tx,ME)} + T_s \right) + \alpha_{ME} P_i T^{(on,tx,ME)} + P^{(rx,ckt)} \left( T^{(on,rx,ME)} + T_s \right)
 \end{aligned}$$



$$E^{(ME)} = \frac{1}{K} \sum_{i=1}^K E_i^{(ME)}$$



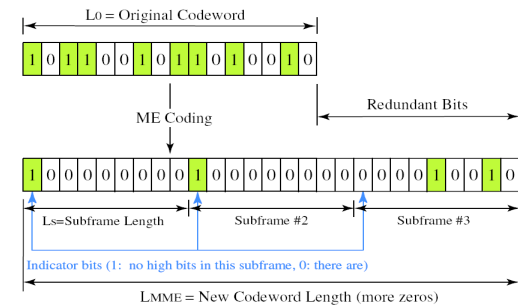


# Average Energy MME Consumption

♣ The energy is function of the BER

$$\begin{aligned}
 E_i^{(MME)} &= E_i^{(tx)} + E_i^{(rx)} \\
 &= P^{(tx,ckt)} \left[ T^{(on,tx,MME)} + T_s \right] + \alpha_{MME} P_i T^{(on,tx,MME)} + \\
 &\quad + P^{(rx,ckt)} \left[ T^{(on,rx,MME)} + (N_i + 1) T_s \right] .
 \end{aligned}$$

$$N_i = N_s [1 - \Pr(b_{ind} = 0) (1 - \Phi_i) - \Pr(b_{ind} = 1) \Phi_i]$$



Receiver activity per MME codeword

$$E^{(MME)} = \frac{1}{K} \sum_{i=1}^K E_i^{(MME)}$$

$$\rho_{dB} = \left( \frac{E^{ME}}{E^{MME}} \right)_{dB}$$

MME Energy Gain



- 
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# Numerical Results

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CC2420 was taken as reference for the energy parameters

$$K = 10$$

Number of transmitter receiver pairs

$$P_l(d_r)|_{\text{dB}} = -55 \text{ dB}$$

Path loss at reference distance

$$G = 64$$

Spreading gain

$$N_0/2|_{\text{dB}} = -174 \text{ dBm}$$

Noise Variance

$$\text{SINR } \gamma = 3.1 \text{ dB}$$

SINR Threshold

$$R_b = 250 \text{ Kbps}$$

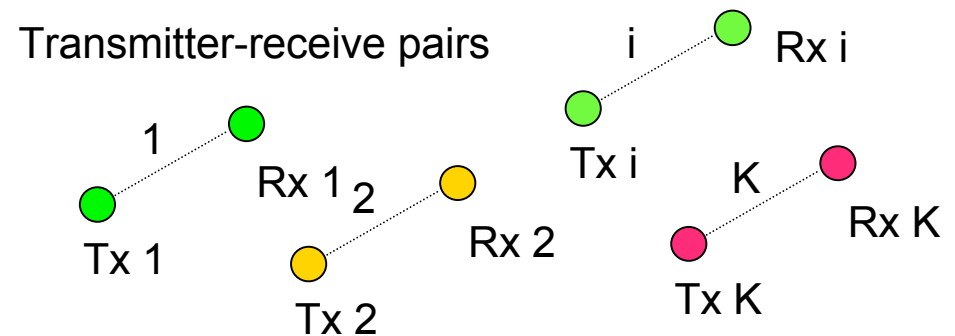
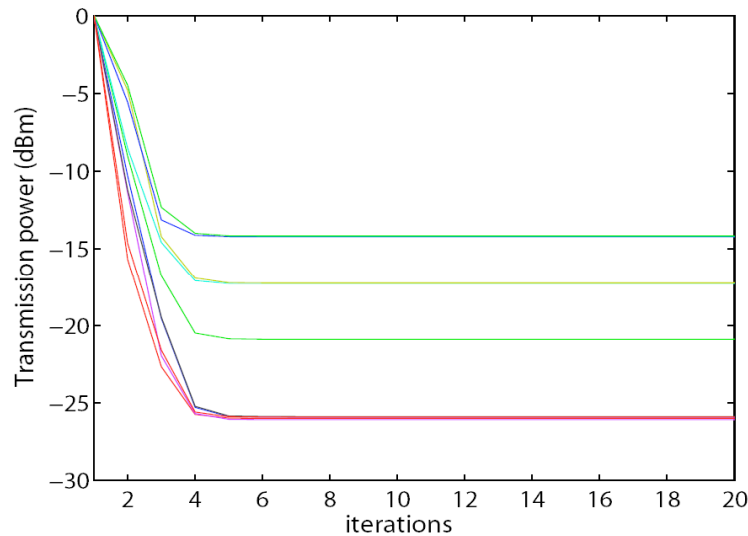
Bit rate





# Radio Power Optimization

- ♣ Convergence of the power minimization algorithm. On the x-axis is reported the number of iterations.



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**Algorithm** *Relaxation Problem*

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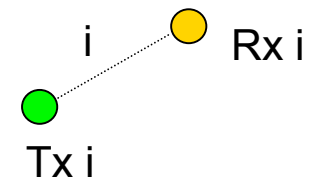
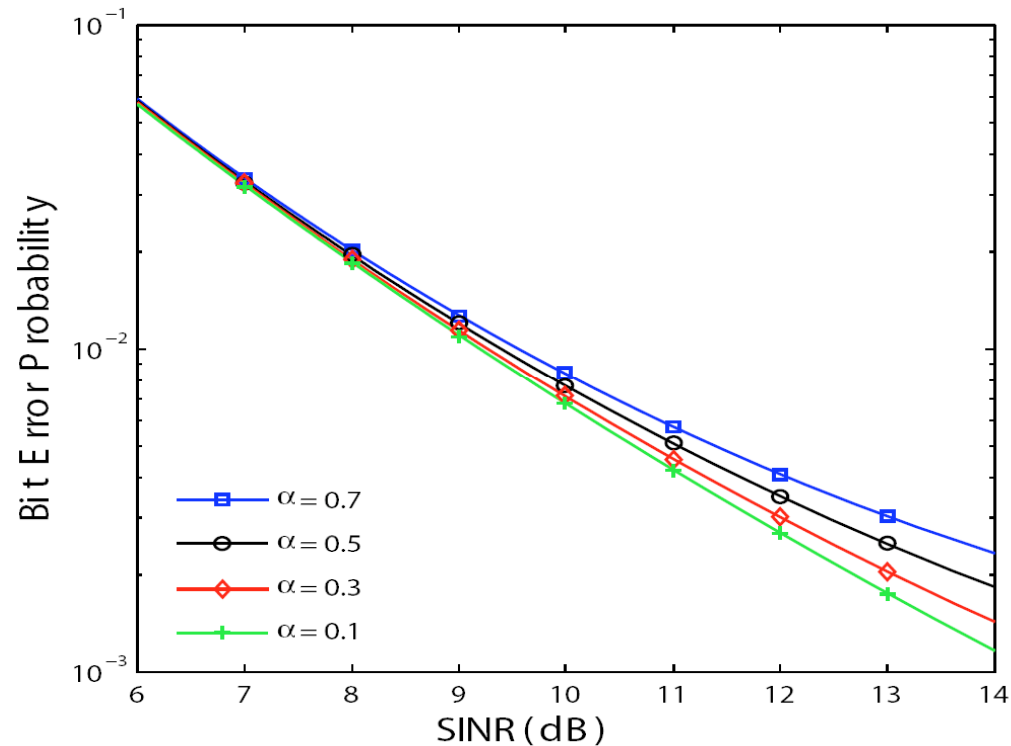
```
1:  $t := 0$ ;  
2:  $\mathbf{n}(t-1) := \mathbf{1}$ ;  
3:  $\mathbf{p}(t-1) := \mathbf{0}$ ;  
4:  $\mathbf{n}(t) := \mathbf{1}$ ;  
5:  $\mathbf{p}(t) := \mathbf{p}_0$ ;  
6: while  $\|\mathbf{p}(t) - \mathbf{p}(t-1)\|_2 \geq \epsilon$  do  
7:   for  $i := 1 : K$  do  
8:      $p_i(t) := I_i(\mathbf{n}_{-i}(t-1), \mathbf{p}_{-i}(t-1))\gamma_i$   
9:   end for;  
10:   $t := t + 1$ ;  
11: end while;
```

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# BER

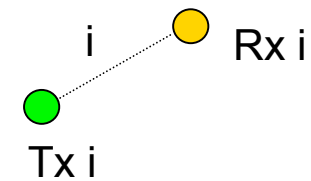
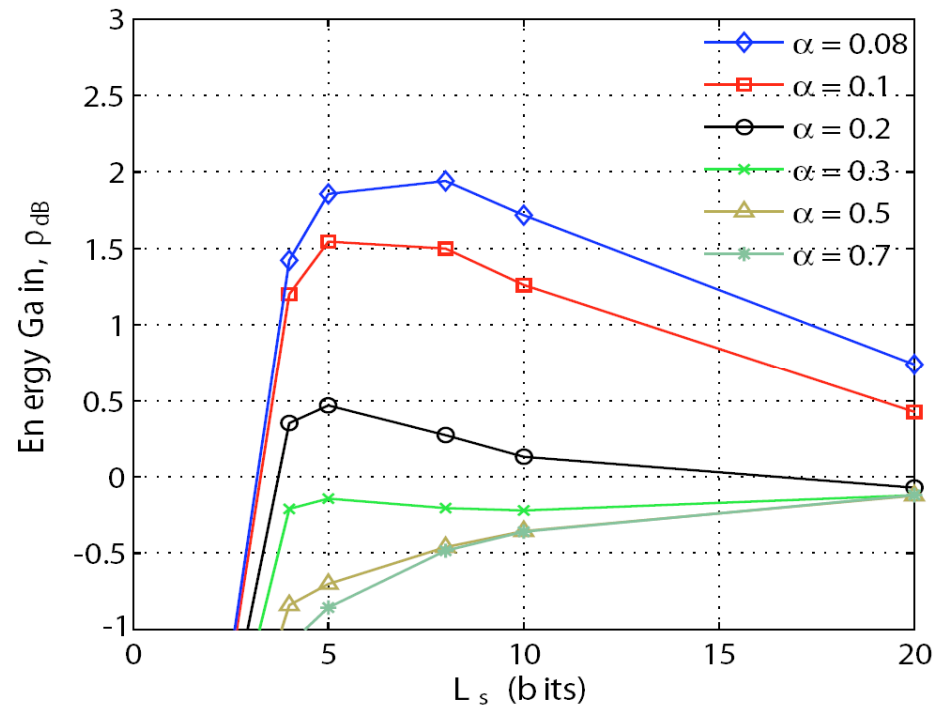
- ♣ Bit error probability for the ME and MME cases (note that they overlap).





# Energy Consumption

- ♣ MME Energy Gain as function of the sub-frame length, for different values of the transmitter activity



$$\rho_{dB} = \left( \frac{E^{ME}}{E^{MME}} \right)_{dB}$$



# Conclusions and Future Work

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- ♣ A general framework for accurate analysis of the Energy Consumption of ME and MME coding has been proposed.
  - Accurate Energy model and wireless propagation scenario.
  - Distributed power minimization strategy.
  - Optimal decision thresholds.
  
- ♣ Future studies
  - delay characterization.
  - distributed estimation.
  - simpler power control (geometric programming...)



# Acknowledgements

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# Questions

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Thank you for your attention!

Any questions?