# Learning and Control

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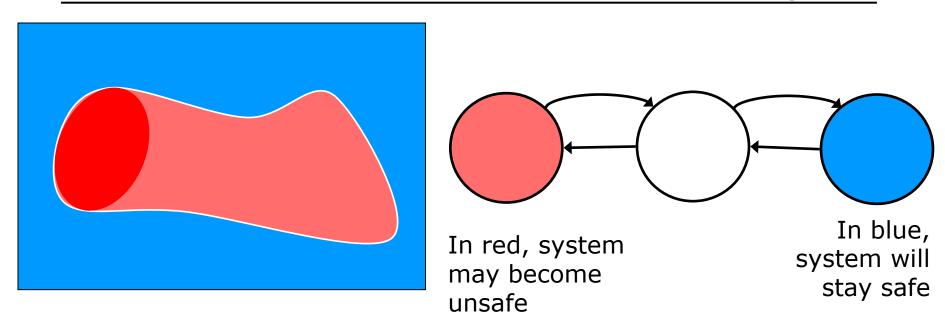


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# System verification and control design

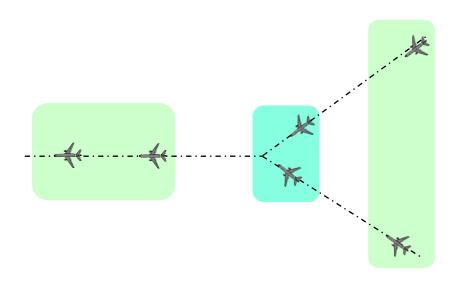


- much of control theory is concerned with certifying system behavior (stability, robustness, reachability...)
- usually performed on simple, abstract models
- tools preclude complex dynamics, such as human behavior, economic implications

## Examples

### Air traffic control

# **Energy Efficient Buildings**





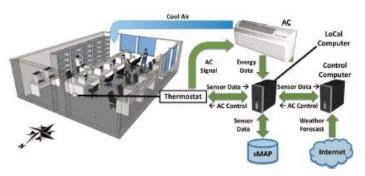
- Controllers, pilots, passengers
- Grouping and conflict classification
- Uncertainty

- Controller, occupants
- Interlinked spaces with time-varying objectives
- Uncertainty

[with Hamsa Balakrishnan]

## **Uncertainty from Humans**

- Interplay between
  - Physics
  - Humans
  - Computation
- Tackling uncertainty will
  - Improve efficiency
  - Increase performance
  - Enhance robustness



## **Smart Buildings**

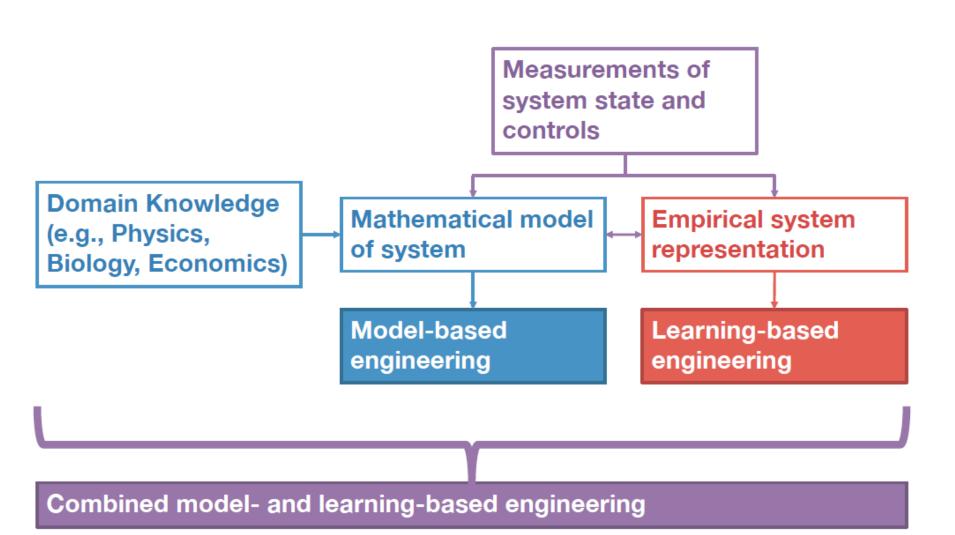
(Aswani, et al., Proc. IEEE, 2011)



High-performance Systems

(Aswani, et al., ACC, 2012)

## Research Philosophy



### Learn models from data...

... but satisfy control requirements while learning

### Control requirements:

- A nominal model with error bounds
- Reachable sets computed to ensure properties hold in worst case
- Reachable sets computed using Model Predictive Control (MPC)

### Performance:

- Use online learning to update model
- Cost function used to generate control action within the safe set
- Insight: performance and constraint satisfaction can be decoupled using reachability analysis
- Learning-based (LB) Model Predictive Control (MPC)

# Constraint satisfaction through Reachability

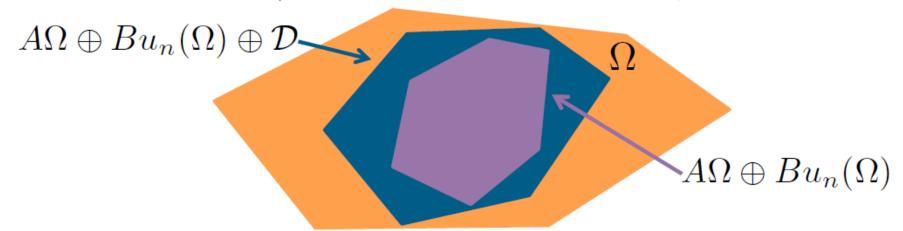
- Reachable set  $\Omega$ 
  - Constraint satisfaction

$$x_n \in \Omega \subseteq \mathcal{X}, u_n(x_n) \in \mathcal{U}, \forall n \geq 0$$

Disturbance invariance

$$\forall x_n \in \Omega \ \exists u_n(x_n) \in \mathcal{U} :$$

$$x_{n+1} = Ax_n + Bu_n + d_n \subseteq \Omega, \forall d_n \in \mathcal{D}$$



## Learning-based Model Predictive Control

- Unknown system dynamics represented using an oracle  $\mathcal{O}$
- At each time step
  - Optimization solved, Oracle updated

**LBMPC** 

### Performance

$$u_{m}^{*} = \arg \min \left\{ J(\tilde{x}_{m+1}, \dots, \tilde{x}_{m+N}, u_{m}, \dots, u_{m+N-1}) \right\}$$
s.t. 
$$\tilde{x}_{n+1} = A\tilde{x}_{n} + Bu_{n} + \mathcal{O}_{m}(\tilde{x}_{n}, u_{n})$$

$$x_{m+k} \in \mathcal{X} \ominus \mathcal{R}_{i}; x_{m+N} \in \mathcal{X}_{N} \ominus \mathcal{R}_{N}$$

$$u_{m+k} = Kx_{m+k} + c_{m+k} \in \mathcal{U} \ominus K\mathcal{R}_{i}$$

$$x_{n+1} = Ax_{n} + Bu_{n}$$

- Cost function
- Learned model
- Constraints and uncertainty
- Original model

Safety

## Learning-based Model Predictive Control

#### **Theorem**

If the reach set can be computed, then the closed-loop system that uses the control input computed by LBMPC satisfies all state and input constraints and is stable.

#### **Theorem**

If the oracle is bounded and continuous, then the value function of the LBMPC optimization problem is continuous.

#### **Theorem**

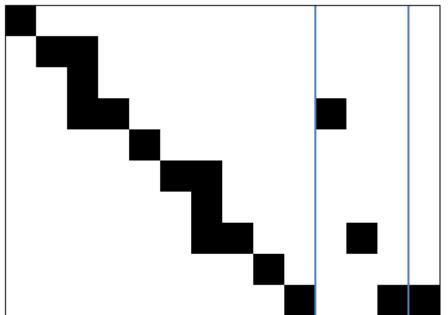
If the reach set can be computed, the linear MPC with the nominal model is asymptotically stable, and the oracle is bounded and continuous; then the closed-loop system is robustly asymptotically stable (RAS) stable with respect to the modeling error and disturbance.

## Example 1: Learning to fly

### Linear model

$$x_{n+1} = Ax_n + Bu_n + d$$

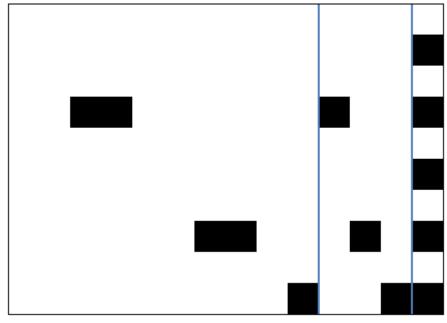
$$A \qquad B \qquad d$$



## Statistics augments physics

$$\mathcal{O}_m = Fx_n + Hu_n + z$$

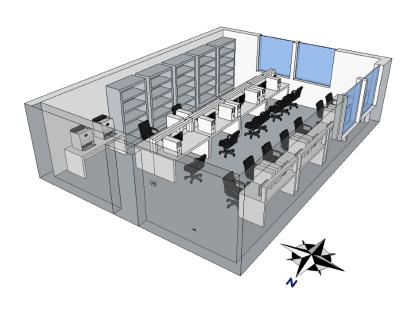
$$F \qquad H$$



# Example 1: Learning to fly

video

# Example 2: Energy-efficient buildings



- 640 sq. ft. computer space
- Networked thermostat
- Newton's law of cooling with heating load



- 141,000 sq. ft. building
- Seven floors of mixed-use space
- Convective cooling with heating load

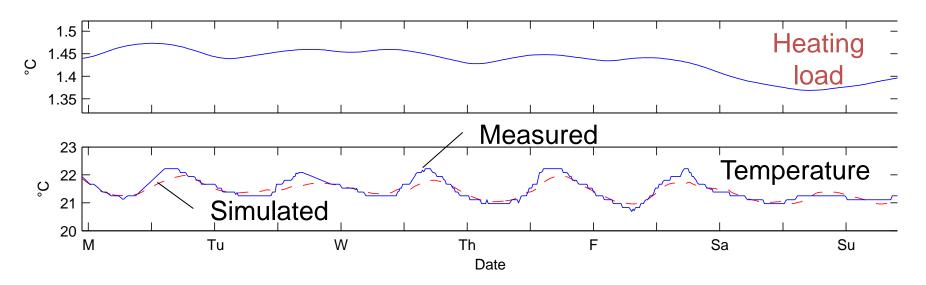
Berkeley Retrofitted and Inexpensive HVAC Testbed for Energy Efficiency (BRITE) [ with Aswani, Culler, Taneja, Krioukov]

## **Temperature Modeling**

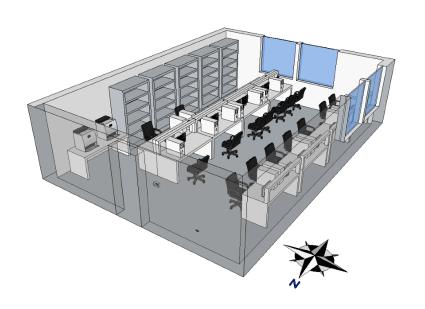
- Semi-parametric regression modeling
  - Parametric: Newton's law of cooling
  - Nonparametric: Heating load

$$T_{n+1} = AT_n + B_1 u_n + B_2 w_n + q_n$$

Estimate heating load using only temperature measurements of thermostat



## **Experiments on BRITE**

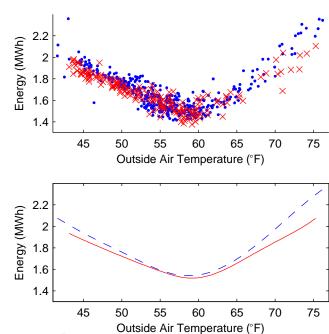


Experiment	Method	Energy
Thermostat Controller	LBMPC Thermostat	23.6 kWh 32.6 kWh
LBMPC Controller	LBMPC	11.8 kWh
	Thermostat	34.5 kWh

- LBMPC provides significant energy savings
- Simulations and experiments used to compare controllers

## **Experiments on BRITE-S**



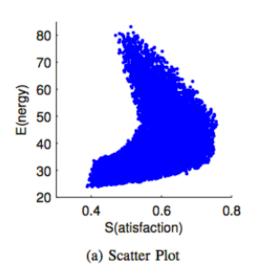


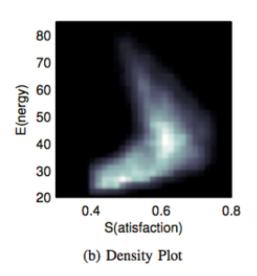
- Comparisons using many experiments and nonparametric hypothesis testing
- 1.5MWh energy saved on average per day
  - Statistically significant (p=0.002)
  - 95% Confidence Interval of 1MWh to 2MWh savings

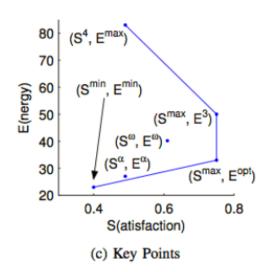
## Incentive Design for Efficient Quality of Service

### **Key Question**

How can incentive schemes that encourage energy-efficient operation of buildings without degradations in quality of service be designed, while also preventing gaming (e.g., moral hazards)?

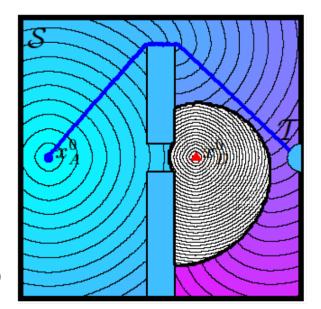


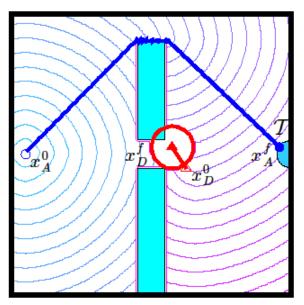




## **Fast Certification**

- Reachability specifications typically exponential in dimension of continuous state space
- Fast approximations of "upper value" and "lower value" using an open loop game:  $\underline{v}(\mathbf{x^0}) \leq \underline{v}(\mathbf{x^0}) \leq V(\mathbf{x^0}) \leq \overline{v}(\mathbf{x^0})$ 
  - Result 1: Open-Loop upper value can be computed exactly [Zhou, Huang, Ding, Takei, Tomlin, submitted 2012]
  - Result 2: A lower bound for the open-loop lower value can be computed [Zhou, Takei, Huang, Tomlin, CDC 2012]



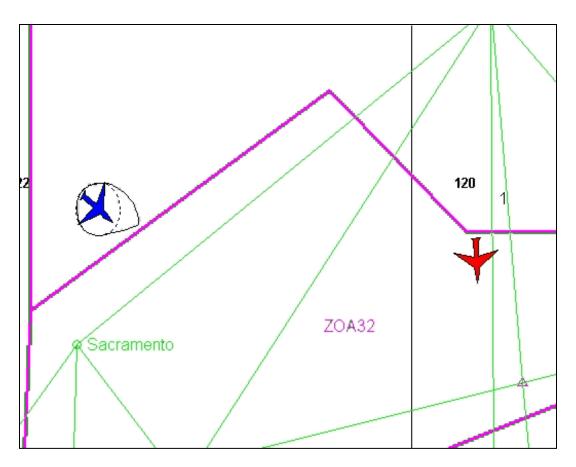


(lower)

(upper)

# Characterizing human interaction

Example: reachability in air traffic control



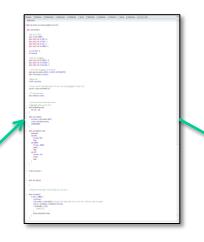
[from Alex Bayen, a long time ago]

## Example 3: Automation to aid controllers

- Infeasible to get data from real controllers
- Most experiments use retired controllers or student volunteers
- Retired controllers are rare, students get bored, where to get more data?



Contrails: Air traffic control game for Android



Trajectories, aircraft states, player inputs

Replay Engine on Server

### A Typical ATC experiment<sup>1</sup>

28 participants168 trials (6 each)

Local US college students

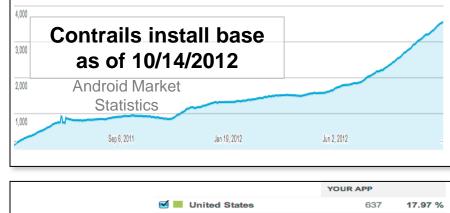
Max individual sample (est): **100** planes

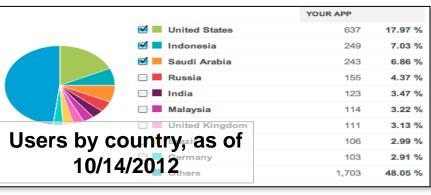
#### **Contrails to date**

**3544** active installs **63,583** games played

10+ countries

Most active user: 9489 planes

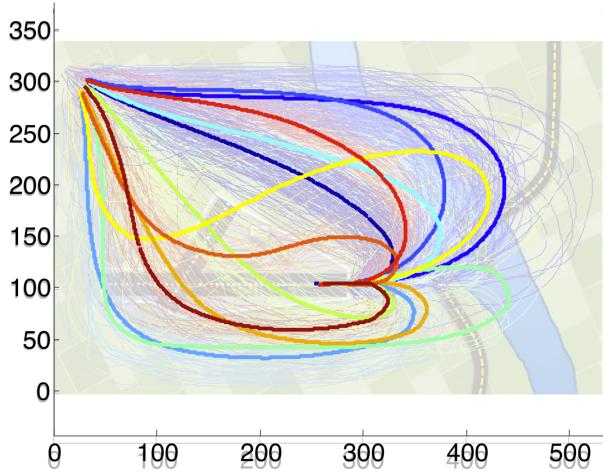






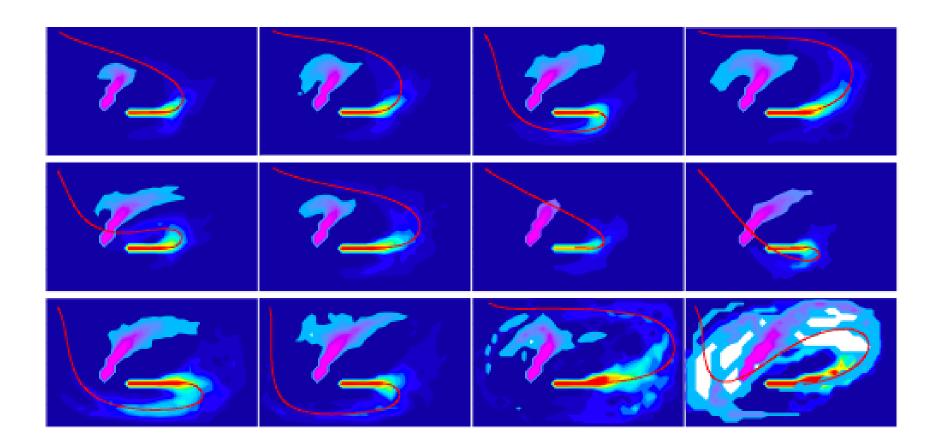
## Modeling using gathered data

- Hypothesized hybrid model for controlled aircraft
- Data is supportive; clustering suggests discrete set of maneuvers used



# Modeling using gathered data

- Predict the maneuver given the airspace
  - Avoidance maneuvers
  - How people sequence moving objects

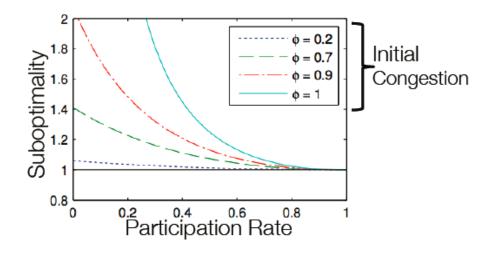


## Analytics and Incentives

- Design of visual big data analytics
  - Encourage sustainable use of systems
  - Improve healthiness and well-being
- Game theory to design incentives
  - Connects groups with different objectives
  - Open problems in computational design



GPS-Traffic Display



[Aswani and Tomlin, ACC 2011; with Krichene, Zhou, Bayen 2013]

## Conclusions and current work

### Reachability-inspired control of hybrid systems

- Control law directly from the reachable set calculation
- Automated controller synthesis for switched systems
  - Under sampling and quantization
- Learning-based control inside reachable sets
  - Physics augmented with learning from data

### Current directions

- Reachable set over-approximation methods
  - Control and "open loop" games allows for use of Fast Marching Methods
- Capturing and using human behavior
- Mechanisms in ATC (with Hamsa)
- Stochastic hybrid systems: Models, Reachability methods, and Trajectory optimization
- Mean-field game representations; principal-agent models (see poster by Balandat and Yang)

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